

**FACULTY OF ENGINEERING & TECHNOLOGY****Third Year (CSE/IT) Examination-Dec-2014****Theory of Computation (Revised)****[Time: THREE Hours]****[Max. Marks: 80]****"Please check whether you have got the right question paper."****N.B**

- 1)Q. no 1 and 6 are compulsory
- 2)Attempt any two questions from Q. No 2 to Q .no 5 and from Q. no. 7 to Q. no 10 of each section.
- 3)Figures to the right indicate full marks.

**SECTION A****Q.1**

Attempt any five from the following

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- a) Define NFA with epsilon transitions. Give suitable example.
- b) Describe the sets for  $(a+b)^*$  and  $(a+b)^+$  state the difference in the two sets.
- c) Define ardeus theorem and state it significance in finite automata
- d) Define mealy machine with example.
- e) What is the relation between finite automata and regular expressions?
- f) Define derivation tree in CFG.
- g) Define CFG and CFH with example.
- h) Distinguish between NFA with epsilon transitions and NFA without epsilon transitions.

**Q.2**

- a) Define ambiguity in CFG. Prove that the given grammar is ambiguous.

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$$\begin{aligned}E &\rightarrow E + E \\E &\rightarrow E - E \\E &\rightarrow E * E \\E &\rightarrow (E) \\E &\rightarrow id\end{aligned}$$

**Q.3**

- b) Using pumping lemma show that  $L = \{ a^n b^n | n \geq 1 \}$  is not regular language.
- a) Construct Moore machine equivalent to Mealy machine given below.

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Present state	Next state	O/P	Next state	O/P
$q_1$	$q_3$	0	$q_2$	0
$q_2$	$q_1$	1	$q_4$	0
$q_3$	$q_2$	1	$q_1$	1
$q_4$	$q_4$	1	$q_3$	0

- b) Convert the given NFA to equivalent DFA

State	$\epsilon$	a	b
$\rightarrow q_0$		$\{q_0, q_1\}$	$\{q_2\}$
$q_1$		$\{q_0\}$	$\{q_1\}$
$\textcircled{q}_2$	-		$\{q_0, q_1\}$

**Q.4**

- a) Minimize the following DFA

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States	$\epsilon$	0	1
$\rightarrow q_1$		$q_2$	$q_6$
$q_2$		$q_1$	$q_3$
$\textcircled{q}_3$		$q_2$	$q_4$
$q_4$		$q_4$	$q_2$
$q_5$		$q_4$	$q_5$
$\textcircled{q}_6$		$q_5$	$q_4$

- b) Find regular expression for the language over  $\{0, 1\}^*$  with set of strings beginning with substring 00. Construct finite automation with the help of regular expression.

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Q.5

Write short notes on.

- i) Chomsky hierarchy
- ii) Applications of FA
- iii) Structural representation of FA.

### SECTION B

Q.6

Attempt any five questions from the following.

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- a) Define CNF and GNF.
- b) What are possibilities of a TM when processing an input string?
- c) Explain the two methods of acceptance of string by PDA.
- d) Define unit production and null production in CFG.
- e) What is the main application of pumping lemma in CFL
- f) Define turingmarline.
- g) State and explain any two properties of CFL.
- h) Eliminate null productions from the following grammar

$$S \rightarrow ABA$$

$$A \rightarrow aA | ^$$

$$B \rightarrow bB | ^$$

Q.7

- a) Construct PDA for the following grammar.

$$S \rightarrow a|b|Sa|Sb|So|Si$$

$$A \rightarrow S|A * A|A + A$$

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- b) Show that  $L = \{a^{n^2} | n \geq 1\}$  is not context free Language.

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Q.8

- a) Consider the grammar below and convert it into Chomsky normal form.

$$S \rightarrow AAA|B$$

$$A \rightarrow aA|B$$

$$B \rightarrow ^$$

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- b) Explain the model of linear bounded automata also state how is LBA different from TM.

Q.9

- a) Explain deterministic push down automata. How does it differ from non deterministicPDA?

- b) Design a Turing machine over  $\{1, b\}$  which can compute a concatenation function over  $\Sigma = \{1\}$ . If a pair of words  $(w_1, w_2)$  is the input, the output has been  $w_1w_2$ .

Q.10

- a) Explain halting problem of Turing machine with suitable diagram.
- b) Construct PDA for the language given below.

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$$L = \{a^n b^n | n \geq 1\}$$